#Unit Five: Operations and Algebraic Thinking

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OVERVIEW

In this unit, students will:

- Explore, understand, and apply the commutative and associative properties as strategies for solving addition problems.
- Share, discuss and compare strategies as a class.
- Connect counting on to solving subtraction problems. For the problem “15 – 7 = ?” they think about the number they have to add to 7 to get to 15.
- Work with sums and differences less than or equal to 20 using the numbers 0 to 20.
- Identify and then apply a pattern or structure in mathematics. For example, pose a string of addition and subtraction problems involving the same three numbers chosen from the numbers 0 to 20, like 4 + 13 = 17 and 13 + 4 = 17.
- Analyze number patterns and create conjectures or guesses.
- Choose other combinations of three numbers and explore to see if the patterns work for all numbers 0 to 20.
- Understand that addition and subtraction are related, and that subtraction can be used to solve problems where the addend is unknown.
- Use the strategies of counting on and counting back to understand number relationships.
- Organize and record results using tallies and tables.
- Determine the initial and the change unknown.

Students develop strategies for adding and subtracting whole numbers based on their prior work with small numbers. They use a variety of models, including discrete objects and length-based models (e.g., cubes connected to form lengths), to model add-to, take-from, put-together, take-apart, and compare situations to develop meaning for the operations of addition and subtraction, and to develop strategies to solve arithmetic problems with these operations. Prior to first grade students should recognize that any given group of objects (up to 10) can be separated into sub groups in multiple ways and remain equivalent in amount to the original group (Ex: A set of 6 cubes can be separated into a set of 2 cubes and a set of 4 cubes and remain 6 total cubes).

Students understand connections between counting and addition and subtraction (e.g., adding two is the same as counting on two). They use properties of addition to add whole numbers and to create and use increasingly sophisticated strategies based on these properties (e.g., —making tens) to solve addition and subtraction problems within 20. By comparing a variety of solution strategies, children build their understanding of the relationship between addition and subtraction. (Ohio DOE)

The standard MCC.1.OA.3 expects teachers to use their understanding of the commutative and associative properties when teaching addition. The students are NOT expected to name or memorize these properties. First grade teachers are laying the foundation and building an understanding of these properties so that students can have formal discussions and utilize names of the properties in later grades.
STANDARDS FOR MATHEMATICAL CONTENT

Represent and solve problems involving addition and subtraction.

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC.1.OA.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

Understand and apply properties of operations and the relationship between addition and subtraction.

MCC.1.OA.3. Apply properties of operations as strategies to add and subtract. Examples: If 8 + 3 = 11 is known, then 3 + 8 = 11 is also known. (Commutative property of addition.) To add 2 + 6 + 4, the second two numbers can be added to make a ten, so 2 + 6 + 4 = 2 + 10 = 12. (Associative property of addition.)

MCC.1.OA.4. Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.

Add and subtract within 20

MCC.1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

MCC.1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 – 4 = 13 – 3 – 1 = 10 – 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 – 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

Work with addition and subtraction equations

MCC.1.OA.7 Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? 6 = 6, 7 = 8 – 1, 5 + 2 = 2 + 5, 4 + 1 = 5 + 2.
The equal sign describes a special relationship between two quantities. In the case of a true equation, the quantities are the same.

MCC.1.OA.8 Determine the unknown whole number in an addition or subtraction equation relating to three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8 + ? = 11, 5 = □ – 3, 6 + 6 = Δ.
Represent and interpret data.
MCC.1.MD.4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

STANDARDS FOR MATHEMATICAL PRACTICE

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important “processes and proficiencies” with longstanding importance in mathematics education.

Students are expected to:

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

***Mathematical Practices 1 and 6 should be evident in EVERY lesson***

ENDURING UNDERSTANDINGS

• Students develop strategies for adding and subtracting whole numbers based on their prior work with small numbers.
• Students use a variety of models, including discrete objects and length-based models (e.g., cubes connected to form lengths), to model add-to, take-from, put-together, take-apart, and compare situations to develop meaning for the operations of addition and subtraction, and to develop strategies to solve arithmetic problems with these operations.
• Students understand connections between counting and addition/subtraction (e.g., adding two is the same as counting on two).
• Students use properties of addition to add whole numbers and to create and use increasingly sophisticated strategies based on these properties (e.g., “making tens”) to solve addition and subtraction problems within 20.
• By comparing a variety of solution strategies, students will build an understanding of the relationship between addition and subtraction.
• Students think of whole numbers between 10 and 100 in terms of tens and ones (especially recognizing the numbers 11 to 19 as composed of a ten and some ones).
**ESSENTIAL QUESTIONS**

- How can we represent a set of objects using numerals?
- What happens when we join two quantities or take one from another?
- How can we find the total when we join two quantities?
- How can we find what is left when we take one quantity from another?
- How can we find the difference when we compare one quantity to another?
- How can we compare one quantity to another?
- How can we represent problem situations?
- What happens when we change the order of numbers when we add (or subtract)? Why?
- How can we show that addition and subtraction are related through fact families?
- How can we use different combinations of numbers and operations to represent the same quantity?
- How can we represent a number using tens and ones?
- How can we represent a number in a variety of ways?

**CONCEPTS AND SKILLS TO MAINTAIN**

- Represent addition and subtraction with objects, fingers, mental images and drawings
- Solve addition and subtraction word problems
- Add and subtract within 10
- Decompose numbers that are less than or equal to 10 in more than one way
- Make a ten from any given number 1-9
- Fluently add and subtract within 5

**SELECTED TERMS AND SYMBOLS**

The following terms and symbols are often misunderstood. This is not an inclusive list and items should not be taught in isolation. However, due to evidence of frequent difficulty and misunderstanding associated with these concepts, instructors should pay particular attention to them and how their students are able to explain and apply them.

The terms below are **for teacher reference only and are not to be memorized by the students**. Teachers should present these concepts to students with models and real life examples. Students should understand the concepts involved and be able to recognize and/or demonstrate them with words, models, pictures, or numbers.

- addition and subtraction within 5, 10, 20, 100, or 1000.
- additive identity property of 0.
- associative property of addition
• commutative property
• computation strategy.
• counting on.
• number line diagram.
• strategies for addition.

STRATEGIES FOR TEACHING AND LEARNING

Addition and Subtraction in Elementary School
• The strategies that students use to solve problems provide important information concerning number sense, and place value.
• It is important to look at more than answers students get. The strategies used provide useful information about what problems to give the next day, and how to differentiate instruction.
• It is important to relate addition and subtraction.
• Student-created strategies provide reinforcement of place value concepts. Traditional algorithms can actually “unteach” place value.
• Student created strategies are built on a student’s actual understanding, instead of on what the book says or what we think/hope they know!
• Students make fewer errors with invented strategies, because they are built on understanding rather than memorization.

Students use various counting strategies, including **counting all, counting on, and counting back** with numbers up to 20. This standard calls for students to move beyond counting all and become comfortable at counting on and counting back. The counting all strategy requires students to count an entire set. The counting and counting back strategies occur when students are able to hold the start number in their head and count on from that number.

<table>
<thead>
<tr>
<th>Add to</th>
<th>Result Unknown</th>
<th>Change Unknown</th>
<th>Start Unknown</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now?</strong></td>
<td>Two bunnies were sitting on the grass. Some more bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to the first two?</td>
<td>Some bunnies were sitting on the grass. Three more bunnies hopped there. Then there were five bunnies. How many bunnies were on the grass before?</td>
<td></td>
</tr>
<tr>
<td>2 + 3 = ?</td>
<td>2 + ? = 5</td>
<td>? + 3 = 5</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Take from</th>
<th>Result Unknown</th>
<th>Change Unknown</th>
<th>Start Unknown</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Five apples were on the table. I ate two apples. How many apples are on the table now?</strong></td>
<td>Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat?</td>
<td>Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before?</td>
<td></td>
</tr>
</tbody>
</table>
Represent and solve problems involving addition and subtraction.
MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC.1.OA.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

Instructional Strategies
One focus in this cluster is for students to discover and apply the commutative and associative properties as strategies for solving addition problems. Students do not need to learn the names for these properties. It is important for students to share, discuss and compare their strategies as a class. The second focus is using the relationship between addition and subtraction as a strategy to solve unknown-addend problems. Students should connect counting on to solving subtraction problems. For the problem “15 – 7 = ?” they think about the number they have to add to 7 to get to 15. First graders should be working with sums and differences less than or equal to 20 using the numbers 0 to 20.
Provide investigations that require students to identify and then apply a pattern or structure in mathematics. For example, pose a string of addition and subtraction problems involving the same three numbers chosen from the numbers 0 to 20, like $4 + 13 = 17$ and $13 + 4 = 17$. These are identified as family families. A fact family is a set of three numbers that can be expressed with an addition or subtraction equation. Fact families help develop an understanding of the relationship between addition and subtraction. Students analyze number patterns and create conjectures or guesses. Have students choose other combinations of three numbers and explore to see if the patterns work for all numbers 0 to 20. Students then share and discuss their reasoning. Be sure to highlight students’ uses of the commutative and associative properties and the relationship between addition and subtraction.

Expand the student work to three or more addends to provide the opportunities to change the order and/or groupings to make tens. This will allow the connections between place-value models and the properties of operations for addition to be seen. Understanding the commutative and associative properties builds flexibility for computation and estimation, a key element of number sense.

Provide multiple opportunities for students to study the relationship between addition and subtraction in a variety of ways, including games, modeling and real-world situations. Students need to understand that addition and subtraction are related, and that subtraction can be used to solve problems where the addend is unknown.

Understand and apply properties of operations and the relationship between addition and subtraction.

MCC.1.OA.3. Apply properties of operations as strategies to add and subtract. Examples: If $8 + 3 = 11$ is known, then $3 + 8 = 11$ is also known. (Commutative property of addition.) To add $2 + 6 + 4$, the second two numbers can be added to make a ten, so $2 + 6 + 4 = 2 + 10 = 12$. (Associative property of addition.)

MCC.1.OA.4. Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.

Instructional Strategies
Provide many experiences for students to construct strategies to solve the different problem types illustrated in Table 1 on page 8. These experiences should help students combine their procedural and conceptual understandings. Have students invent and refine their strategies for solving problems involving sums and differences less than or equal to 20 using the numbers 0 to 20. Ask them to explain and compare their strategies as a class.

Provide multiple and varied experiences that will help students develop a strong sense of numbers based on comprehension – not rules and “tricks” that lead to memorization without
understanding. Number sense is a blend of comprehension of numbers and operations and fluency with numbers and operations. Students gain computational fluency (using efficient and accurate methods for computing) as they come to understand the role and meaning of arithmetic operations in number systems.

Primary students come to understand addition and subtraction as they connect counting and number sequence to these operations. Addition and subtraction also involve part to whole relationships. Students’ understanding that the whole is made up of parts is connected to decomposing and composing numbers.

Provide numerous opportunities for students to use the counting on strategy for solving addition and subtraction problems. For example, provide a ten frame showing 5 colored dots in one row. Students add 3 dots of a different color to the next row and write $5 + 3$. Ask students to count on from 5 to find the total number of dots. Then have them add an equal sign and the number eight to $5 + 3$ to form the equation $5 + 3 = 8$. Ask students to verbally explain how counting on helps to add one part to another part to find a sum.

\[
\begin{array}{cccc}
\bullet & \bullet & \bullet & \bullet \\
\blacklozenge & \blacklozenge & \blacklozenge & \blacklozenge \\
\end{array}
\]

\[5 + 3\]
\[5...6,7,8\]

Work with addition and subtraction equations

MCC.1.OA.7 Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? $6 = 6$, $7 = 8 – 1$, $5 + 2 = 2 + 5$, $4 + 1 = 5 + 2$.

The equal sign describes a special relationship between two quantities. In the case of a true equation, the quantities are the same.

MCC.1.OA.8 Determine the unknown whole number in an addition or subtraction equation relating to three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 + ? = 11$, $5 = □ – 3$, $6 + 6 = △$.

Instructional Strategies

Provide opportunities for students to use objects of equal weight and a number balance to model equations for sums and differences less than or equal to 20 using the numbers 0 to 20. Give students equations in a variety of forms that are true and false. Include equations that show the identity property, commutative property of addition, and associative property of addition. Students need not use formal terms for these properties. Examples are provided for teacher understanding, not student expectations.
Ask students to determine whether the equations are true or false and to record their work with drawings. Students then compare their answers as a class and discuss their reasoning. Present equations recorded in a nontraditional way, like $13 = 16 - 3$ and $9 + 4 = 18 - 5$, then ask, “Is this true?” Have students decide if the equation is true or false. Then as a class, students discuss their thinking that supports their answers.

Provide situations relevant to first graders for these problem types illustrated in Table on page 8: Add to / Result Unknown, Take from / Start Unknown, and Add to / Result Unknown. Demonstrate how students can use graphic organizers, similar to the triangle math concept below, to help them think about problems. The triangle math concept shows a sum with diagonal lines going down to connect with the two addends, forming a triangular shape. It shows two known quantities and one unknown quantity. Use various symbols, such as a square, to represent an unknown sum or addend in a horizontal equation. For example, here is a Take from / Start Unknown problem situation such as: Some markers were in a box. Matt took 3 markers to use. There are now 6 markers in the box. How many markers were in the box before? The teacher draws a square to represent the unknown sum and diagonal lines to the numbers 3 and 6.

Have students practice using the triangle math concept to organize their solutions to problems involving sums and differences less than or equal to 20 with the numbers 0 to 20. Then ask them to share their reactions to using this concept.

**Represent and interpret data.**

**MCC.1.MD.4.** Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

**Instructional Strategies**

In first grade, the students will sort a collection of items in up to three categories. Then ask questions about the number of items in each category and the total number of items. Also ask students to compare the number of items in each category. The total number of items to be sorted should be less than or equal to 100 to allow for sums and differences less than or equal to 100 using the numbers 0 to 100. Connect to the geometry content studied in Grade 1. Provide categories and have students sort identical collections of different geometric shapes. After the shapes have been sorted, ask these questions: How many triangles are in the collection? How many rectangles are there? How many triangles and rectangles are there? Which category has the most items? How many more? Which category has the least? How many less? Students can create a Venn diagram after they have had multiple experiences with sorting objects according to
given categories. The teacher should model a Venn diagram several times before students make their own. A Venn diagram in Grade 1 has two or three labeled loops or regions (categories). Students place items inside the regions that represent a category that they chose. Items that do not fit in a category are placed outside of the loops or regions. Students can place items in a region that overlaps the categories if they see a connection between categories. Ask questions that compare the number of items in each category and the total number of items inside and outside of the regions.

Add and subtract within 20
MCC.1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

MCC.1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 – 4 = 13 – 3 – 1 = 10 – 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 – 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

Fluency
Fluency means:

- accuracy (correct answer)
- efficiency (within 4-5 seconds)
- flexibility (using strategies such as making 5 or making 10)

The standards in this unit call for fluency as well as requiring students to use a variety of strategies when adding and subtracting numbers within 20. Students should have ample experiences modeling these operations before working on fluency. Teacher could differentiate using smaller numbers.

It is important to move beyond the strategy of counting on, which is considered a less important skill than the ones here in MCC.1.OA.6. Many times teachers think that counting on is all a child needs, when it is really not much better skill than counting all and can becomes a hindrance when working with larger numbers.

Example: 8 + 7 = ___

<table>
<thead>
<tr>
<th>Student 1: Making 10 and Decomposing a Number</th>
<th>Student 2: Creating an Easier Problem with Known Sums</th>
</tr>
</thead>
<tbody>
<tr>
<td>I know that 8 plus 2 is 10, so I decomposed (broke) the 7 up into a 2 and a 5. First I added 8 and 2 to get 10, and then added the 5 to get 15. 8 + 7 = (8 + 2) + 5 = 10 + 5 = 15</td>
<td>I know 8 is 7 + 1. I also know that 7 and 7 equal 14 and then I added 1 more to get 15. 8 + 7 = (7 + 7) + 1 = 15</td>
</tr>
</tbody>
</table>
Example: 14 – 6 = ___

**Student 1: Decomposing the Number You Subtract**
I know that 14 minus 4 is 10 so I broke the 6 up into a 4 and a 2. 14 minus 4 is 10. Then I take away 2 more to get 8.

\[ 14 - 6 = (14 - 4) - 2 = 10 - 2 = 8 \]

**Student 2: Relationship between Addition and Subtraction**
6 + □ is 14. I know that 6 plus 8 is 14, so that means that 14 minus 6 is 8.

\[ 6 + 8 = 14 \text{ so } 14 - 6 = 8 \]

Algebraic ideas underlie what students are doing when they create equivalent expressions in order to solve a problem or when they use addition combinations they know to solve more difficult problems. Students begin to consider the relationship between the parts. For example, students notice that the whole remains the same, as one part increases the other part decreases. 5 + 2 = 4 + 3 (N.C. Dept. of Public Instruction)
### ADDITION STRATEGIES

| Count All | 5 + 4 = 9  
<table>
<thead>
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</thead>
<tbody>
<tr>
<td>Count 5, then count 4, then count them all</td>
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</tr>
<tr>
<td>1 2 3 4 5</td>
<td>1 2 3 4</td>
</tr>
<tr>
<td>1 2 3 4 5 6 7 8 9</td>
<td></td>
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</tbody>
</table>

| Facts with Zero | 4 + 0 = 4  
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<tr>
<td>It is important for children not to over generalize that addition facts always end with a number larger than what they began with. Drawings should be used to illustrate that there are two parts and one part is empty.</td>
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</table>

| Count on | 3 + 2 = 5  
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<tbody>
<tr>
<td>(one more than/two more than)</td>
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<tr>
<td>Start at 3, then continue counting 4, 5. The student should not go back to one.</td>
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</tbody>
</table>

| Doubles | 4 + 4 = 8  
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</thead>
<tbody>
<tr>
<td>2 + 2 = 4</td>
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</tbody>
</table>

| Doubles Plus or Minus | 5 + 6 = 11  
<table>
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<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>5 + 5 + 1 = 11 OR 6 + 6 – 1 = 11</td>
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</tbody>
</table>

| Doubles are much easier for students to remember and are useful in fact fluency |

| Ten Frame Facts | 7 + 3 = 10  
<table>
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</tr>
</thead>
<tbody>
<tr>
<td>3 + 7 = 10</td>
<td></td>
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</tbody>
</table>

| Working with Fives | 6 + 8 = 14  
<table>
<thead>
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<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>5 + 1 + 5 + 3</td>
<td></td>
</tr>
<tr>
<td>10 + 4 = 14</td>
<td></td>
</tr>
</tbody>
</table>

| Making Tens | 8 + 4 = 12  
<table>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>2 + 2 = 4</td>
<td></td>
</tr>
<tr>
<td>10 + 2 = 12</td>
<td></td>
</tr>
</tbody>
</table>

| Using Compensation | 7 + 4 = 11  
|                   |-----------|
| (making friendly numbers) |
| Think |
| 10 + 4 = 14 |
| 14 - 3 = 11 |

Children can compensate by adding or subtracting quantities to/from one addend in order to make a friendly number. At the end, the inverse operation is applied.
Concrete

<table>
<thead>
<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>Allow students to work at their seat with various manipulatives (red and yellow counters, buttons, connecting cubes, square tiles, etc.) to help them find the number of kids left outside. Some students will need to continue to physically act out the problem multiple times before they are able to use manipulatives to represent objects within the problem.</td>
<td>Once students have grasped the Concrete representation of the problem, they will be ready to create pictures to represent the problem. Allow students to use crayons, pencils, and paper to draw a picture to solve the problem. Allow students to use picture representations that make sense to them (dots, squares, circles, tally marks, actual friends, etc.)</td>
<td>First grade students should begin creating number sentences to describe their story problems after the use of manipulatives and/or the creation of a picture. <strong>Students should be introduced to the terms subtraction, difference, and number sentence throughout this unit.</strong></td>
</tr>
</tbody>
</table>

**Stage Description**

**Suggested Questions**

- How can we show/represent this?
- How many counters are you starting with? Why?
- How many counters are you taking away? Why?
- Can you explain to me how you are using your counters to help you figure out how many friends are left?
- What strategies are you using to help you find out how many friends are left?
- Is your neighbor finding the number of friends left a different way? Can you do it a different way?
- How did you find out how many friends were left? Can you explain that to a neighbor?

**Representational**

<table>
<thead>
<tr>
<th>Suggested questions include:</th>
<th>Suggested questions include: (In teacher modeling, use dots, etc. to show various ways to represent friends to help students not get bogged down with pictures.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>- How can we show/represent this?</td>
<td></td>
</tr>
<tr>
<td>- How many counters are you starting with? Why?</td>
<td></td>
</tr>
<tr>
<td>- How many counters are you taking away? Why?</td>
<td></td>
</tr>
<tr>
<td>- Can you explain to me how you are using your counters to help you figure out how many friends are left?</td>
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<tr>
<td>- What strategies are you using to help you find out how many friends are left?</td>
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<tr>
<td>- Is your neighbor finding the number of friends left a different way? Can you do it a different way?</td>
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</tr>
<tr>
<td>- How did you find out how many friends were left? Can you explain that to a neighbor?</td>
<td></td>
</tr>
<tr>
<td>- How can we show/represent this story?</td>
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</tr>
<tr>
<td>- Describe your picture for me.</td>
<td></td>
</tr>
<tr>
<td>- Do you think a friend would be able to make sense of your picture?</td>
<td></td>
</tr>
<tr>
<td>- How many friends did you draw?</td>
<td></td>
</tr>
<tr>
<td>- How did you show the friends that left for lunch?</td>
<td></td>
</tr>
<tr>
<td>- What strategies are you using to help you subtract/take away the friends that left?</td>
<td></td>
</tr>
<tr>
<td>- How did you find the number of friends that were still outside?</td>
<td></td>
</tr>
<tr>
<td>- Can you think of a different way to find out how many friends were outside?</td>
<td></td>
</tr>
<tr>
<td>- Did your neighbor solve it the same? Instead of acting out the story what could we use to represent the friends?</td>
<td></td>
</tr>
<tr>
<td>- Are there any objects I could use to help me find out how many friends were still outside?</td>
<td></td>
</tr>
<tr>
<td>- Is there a way you could have solved this problem differently? How do you know?</td>
<td></td>
</tr>
</tbody>
</table>

**Abstract**

<table>
<thead>
<tr>
<th>As students are creating number sentences for their story problems, suggested questions include:</th>
</tr>
</thead>
<tbody>
<tr>
<td>- Which number did you subtract from? Why?</td>
</tr>
<tr>
<td>- How many did you subtract from ______?</td>
</tr>
<tr>
<td>- Why did you subtract ______ - ______ and not the other way around?</td>
</tr>
<tr>
<td>- Which number did you place first when you subtracted?</td>
</tr>
<tr>
<td>- Will I get the same answer if I change the order of numbers when I subtract?</td>
</tr>
<tr>
<td>- How did you know this was a subtraction problem?</td>
</tr>
<tr>
<td>- Which sign did you use? Why?</td>
</tr>
<tr>
<td>- What is the difference? What does that mean?</td>
</tr>
<tr>
<td>- How did you find the difference? What strategies did you use?</td>
</tr>
<tr>
<td>- How can we show/represent this story?</td>
</tr>
<tr>
<td>- How can you check the difference to make sure it is correct?</td>
</tr>
<tr>
<td>- Is there another way you could have solved this problem?</td>
</tr>
<tr>
<td>- Did your neighbor solve it the same way you did or differently? How do you know?</td>
</tr>
</tbody>
</table>
COMMON MISCONCEPTIONS

Addition and subtraction can be divided into four categories: join problems, separate problems, part-whole problems, and compare problems (see Table 1 on page 8). Within these four types of problems, most educators focus on addition and subtract when the result is unknown, this leads to the understanding that addition is “put together” and subtraction means to “take away”. This is a major misconception and limits the students’ understanding.

One way to prevent development of this misunderstanding is to provide problem based story problems in which the students are attempting to solve not only the result but also the change, and the initial. (Van De Walle, pages 67-71)

“What might a good lesson look like for second grade [first grade] that is built around word problems? The answer comes more naturally if you think about students not just solving the problems but also using words, pictures, and numbers to explain how they went about solving the problem and why they think they are correct. Children should be allowed to use whatever physical materials they feel they need to help them, or they can just simply draw pictures. Whatever they put on paper should explain what they did well enough to allow someone else to understand it. Allow at least a half page of space for a problem.” (VDW, page 71)

Once students have an understanding of numbers, they are then more prepared to perform and comprehend operations. A common misconception is that the commutative property applies to subtraction. After students have discovered and applied the commutative property for addition, ask them to investigate whether this property works for subtraction. Have students share and discuss their reasoning and guide them to conclude that the commutative property does not apply to subtraction.

Many students misunderstand the meaning of the equal sign. The equal sign means “is the same as” but most primary students believe the equal sign tells you that the “answer is coming up” to the right of the equal sign. This misconception is over-generalized by only seeing examples of number sentences with an operation to the left of the equal sign and the answer on the right. First graders need to see equations written multiple ways, for example $5 + 7 = 12$ and $12 = 5 + 7$. (Ohio DOE)

Another misconception that many students have is that it is valid to assume that a key word or phrase in a problem suggests the same operation will be used every time. For example, they might assume that the word left always means that subtraction must be used to find a solution. Providing problems in which key words like this are used to represent different operations is essential. For example, the use of the word left in this problem does not indicate subtraction as a solution method: Seth took the 8 stickers he no longer wanted and gave them to Anna. Now Seth has 11 stickers left. How many stickers did Seth have to begin with? Students need to analyze word problems and avoid using key words to solve them. (Ohio DOE)
EVIDENCE OF LEARNING

By the conclusion of this unit, students should be able to demonstrate the following competencies:

- Represent and solve problems involving addition and subtraction.
- Understand and apply properties of operations and the relationship between addition and subtraction.
- Add and subtract within 20.
- Work with addition and subtraction equations.
- Represent and interpret data.
<table>
<thead>
<tr>
<th>Task Name</th>
<th>Task Type</th>
<th>Content Addressed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Developing Meaning Using Story Problems:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Result Unknown</td>
<td>Constructing</td>
<td>Problem solving with the result unknown</td>
</tr>
<tr>
<td>Lots of Dots</td>
<td>Task</td>
<td>Composing and decomposing of numbers</td>
</tr>
<tr>
<td>What Numbers Can You Make?</td>
<td>Constructing</td>
<td>Composing and Decomposing of numbers</td>
</tr>
<tr>
<td>Wheel Shop</td>
<td>Performance</td>
<td>Problem solving</td>
</tr>
<tr>
<td>Digging Dinosaurs</td>
<td>Performance</td>
<td>Problem solving</td>
</tr>
<tr>
<td>Developing Meaning Using Story Problems:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Change Unknown</td>
<td>Constructing</td>
<td>Problem solving with the change unknown</td>
</tr>
<tr>
<td>Shape Pounds</td>
<td>Task</td>
<td>Writing numbers sentences with a shape representing an unknown</td>
</tr>
<tr>
<td>Fact Families to Ten</td>
<td>Scaffolding</td>
<td>Relating addition to subtraction</td>
</tr>
<tr>
<td>Developing Meaning Using Story Problems:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Initial Unknown</td>
<td>Constructing</td>
<td>Problem solving with the initial unknown</td>
</tr>
<tr>
<td>Domino Fact Family</td>
<td>Practice</td>
<td>Relating addition to subtraction</td>
</tr>
<tr>
<td>Candy</td>
<td>Practice</td>
<td>Graphing</td>
</tr>
<tr>
<td>Culminating Task : Atlanta Zoo</td>
<td>Culminating</td>
<td>Problem solving, working with unknowns, writing number sentences</td>
</tr>
</tbody>
</table>

Georgia Department of Education
Common Core Georgia Performance Standards Framework
First Grade Mathematics • Unit 5

MATHEMATICS • GRADE 1 • UNIT 5: Operations and Algebraic Thinking
Georgia Department of Education
Dr. John D. Barge, State School Superintendent
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CONSTRUCTING TASK: Developing Meaning by using Story Problems: Result Unknown
Approximately 3 days

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

The goal for this lesson is to expose students to real world problems, using the level of understanding (concrete, representational, or abstract) that each student needs. (see CRA Table on page 15) Addition and subtraction can be divided into four categories: join problems, separate problems, part-whole problems, and compare problems (see Table 1 on page 8). Within these four types of problems, most educators focus on addition and subtract when the result is unknown, this leads to the understanding that addition is “put together” and subtraction means to “take away”. This is a major misconception and limits the students’ understanding. One way to prevent development of this misunderstanding is to provide problem based story problems in which the students are attempting to solve not only for the result but also the change, and the initial.

Students should not complete a multitude of problems within one class period, rather they should work in depth with as few as one problem that they can know and understand completely. Students do not need to know the names of the different types of problems but they should have experience in solving all of the different types. This lesson should not be looked at to be completed in one session, these questions should be readdressed throughout this unit and continue throughout the mathematics curriculum across the year and grade levels.
ESSENTIAL QUESTIONS

- What happens when we join two quantities or take one from another?
- How can we find the total when we join two quantities?
- How can we find what is left when we take one quantity from another?
- What happens when we change the order of numbers when we add (or subtract)? Why?

MATERIALS

- Paper
- Various Manipulatives (examples: counters, based ten blocks, arithmetic rack, etc.)
- Pencils
- Crayons
- Types of Problems (cut out)
- Fill the Tree Game
- Dice
- Small counters

GROUPING

Flexible Grouping (based on student needs) Depending on the story problem, this task could be solved with students working as a whole-class, small groups, or independently.

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
The teacher will tell a story similar to the one suggested and engage in conversation about the questions provided. Continue questioning as needed until the students can answer the questions and understand what is happening in the story.

Five friends are playing outside, five more join them.
- Will that make more or less friends playing together? How do you know?
- What can you do to figure out the total number of friends playing outside now?

Later on, 3 friends had to go inside for lunch.
- How many did that leave playing outside?
- Are there more students inside or outside now? How do you know?
- What did you do to figure it out?
- How was that different from what we did at the beginning of the story, in other words, how did the “actions” for solving or thinking about the problem change?
- How could we use a number line to model the actions in this story?”
Part II
Sample problems have been provided. Copy the problems, cut them out to give to students and/or flexible groups. Each set can be done within small groups or within centers/work stations. The sample word problems are designed to give a conceptual understanding of addition and subtraction of two numbers. Students should explore these problems using the CRA model. Refer to the CRA table on page 15 for explanation and questioning.

- C- Concrete: Using Manipulatives (acting out)
- R- Representational: Drawing Pictures
- A- Abstract: Creating Number Sentences

“In the classroom, this approach is a facilitating framework for students to create meaningful connections between concrete, representational, and abstract levels of thinking and understanding. Students’ learning starts out with visual, tangible, and kinesthetic experiences to establish basic understanding, and then students are able to extend their knowledge through pictorial representations (drawings, diagrams, or sketches) and then finally are able to move to the abstract level of thinking, where students are exclusively using mathematical symbols to represent and model problems.” Hauser, Jane. Concrete-representational-abstract instructional approach.

Suggestion for lesson pacing:
- Day one- Students will solve problems within small groups
- Day two- Students will solve problems within partners
- Day three- Students will solve problems independently

The problems listed below are examples from the four types of addition/subtraction problems. The numbers and topics of each problem can be adjusted based on the interest and ability of your students. All four types of problems should be focused in a variety of ways.

Join Problems:
When joining two quantities, three different amounts are used: the initial amount, the change amount, and the result amount (or whole). (VDW)
Example: The other day I saw 5 dogs chasing a ball in the park. Then, three more dogs came and joined them playing ball. How many dogs were playing in the park? 5+3=____

Separate Problems:
Within separate problems, your initial amount is the whole. This differs from a joining problem because within a joining problem your result is your whole. (VDW)
Example: Jack has 11 lizards in a cage. 4 escape. How many are left? 11- 4= ____
Part-Part-Whole is the combing of two quantities to create a whole. The combination can take place physically, or it can be asked to be completed mentally.
Example: Jessica has 7 nickels and 3 dimes. How many coins does Jessica have all together? 7+3=____
Comparing Problems:
Comparing problems do not focus on the operation, but rather the relationship between two quantities. This relationship can be stated or it can be implied by using terms of greater than or less than. (VDW)

Example: Sarah has 7 dogs. Katie has 12 dogs. How many more dogs does Katie have than Sarah? 12-7=_____ or 7+____=12

Part III
Students will play “Fill the Tree” with a partner. Each group will need one game board, different color chips or counters for each player and a pair of 6-sided dice. Each player will determine the color chips or counters they will be. Player one will roll the dice, find the sum, and cover the sum with a chip or counter. Player two will repeat the process. Players will take turns until the board is covered. The player to cover the last spot wins. If a sum is already covered the player loses that turn.

FORMATIVE ASSESSMENT QUESTIONS
See included within the CRA table on page 15 of this unit.

DIFFERENTIATION

Extension:
• Allow students to work with numbers larger than 20 without regrouping.
• Ask students to create and solve their own story problems.

Note: Students typically create addition problems. Check students’ problems to make sure they are creating subtraction problems too.

Intervention
• Allow students to work through the stages at a pace that is appropriate to their developmental level. This will provide students with the remediation they need to understand the concept of comparing numbers. Continue to allow them to work with manipulatives as much as needed. At times, partner them with students who are very articulate about their mathematical thinking so they can hear (through conversations) how these students have made sense of the problems.
### Join: Result Unknown

<table>
<thead>
<tr>
<th>The other day I saw 6 dogs chasing a ball in the park. Then, seven more dogs came and joined them playing ball. How many dogs were playing in the park? 6+7=____</th>
<th>There were three people swinging on the swings. One more person joined them. How many children are on the swings? 3+1=___</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Separate: Result Unknown</strong></td>
<td></td>
</tr>
<tr>
<td>There were thirteen chattering monkeys. Five fell asleep. How many monkeys are still chattering? 13-5=__</td>
<td>Pete has 20 mice in a cage. 12 escape. How many are left? 20-12=___</td>
</tr>
<tr>
<td>There were eight bunnies at the pet store. Three went home with a new family. How many bunnies were still at the pet store? 8-3=__</td>
<td>Today at lunch I had twelve chicken nuggets on my tray. I ate seven of my chicken nuggets. How many did I not eat? 12-7=___</td>
</tr>
<tr>
<td>Sarah and Katie had 15 gumballs. Sarah ate 6 of the gumballs. How many are left for Katie? 15-6=__</td>
<td></td>
</tr>
</tbody>
</table>
### Part-Part-Whole: Whole Unknown

<table>
<thead>
<tr>
<th>Tony has 8 pennies and 5 dimes. How many coins does Tony have all together? 8+5=___</th>
<th>Cecil has 10 baseball cards and Anthony has 8 baseball cards. The boys put all their baseball cards into one box. How many baseball cards will be in their box? 10+8=____</th>
</tr>
</thead>
<tbody>
<tr>
<td>How many more kittens does the first litter have? 11-6=___ or 6+___=11</td>
<td></td>
</tr>
<tr>
<td>In my bag of candy, I have thirteen yellow candies and eight red candies. How many more red candies do I have than yellow candies? 13-8=___ or 8+___=13</td>
<td></td>
</tr>
</tbody>
</table>

### Compare: Difference Unknown

<table>
<thead>
<tr>
<th>One litter has eleven kittens. Another litter has six kittens. How many more kittens does the first litter have? 11-6=___ or 6+___=11</th>
<th>Pete has 9 mice. Max has 13 mice. How many more mice does Max have than Pete? 13-9=___ or 9+___=13</th>
</tr>
</thead>
<tbody>
<tr>
<td>In my bag of candy, I have thirteen yellow candies and eight red candies. How many more red candies do I have than yellow candies? 13-8=___ or 8+___=13</td>
<td></td>
</tr>
<tr>
<td>I picked some flowers for my mother. I gave her twenty daisies and fifteen roses. How many more daisies did I give her than roses? 20-15=___ or 15+___=20</td>
<td></td>
</tr>
</tbody>
</table>
Fill the Tree

Materials: game board, different color chips or counters for each player, pair of 6-sided dice.

Number of Players: Two – both players will use one game board

Directions: Each player will determine the color chips or counters they will be. Player one will roll the dice, find the sum, and cover the sum with a chip or counter. Player two will repeat the process. Players will take turns until the board is covered. The player to cover the last spot wins. If a sum is already covered the player loses that turn.
**Scaffolding: Lots of Dots**
Approximately 2-3 Days Adapted from NCTM Navigating Through Algebra K-2

**STANDARDS FOR MATHEMATICAL CONTENT**

**MCC.1.OA.3.** Apply properties of operations as strategies to add and subtract. Examples: If $8 + 3 = 11$ is known, then $3 + 8 = 11$ is also known. (Commutative property of addition.) To add $2 + 6 + 4$, the second two numbers can be added to make a ten, so $2 + 6 + 4 = 2 + 10 = 12$. (Associative property of addition.)

**MCC.1.OA.4.** Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.

**MCC.1.OA.5.** Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

**MCC.1.OA.6** Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., $8 + 6 = 8 + 2 + 4 = 10 + 4 = 14$); decomposing a number leading to a ten (e.g., $13 - 4 = 13 - 3 - 1 = 10 - 1 = 9$); using the relationship between addition and subtraction (e.g., knowing that $8 + 4 = 12$, one knows $12 - 8 = 4$); and creating equivalent but easier or known sums (e.g., adding $6 + 7$ by creating the known equivalent $6 + 6 + 1 = 12 + 1 = 13$).

**STANDARDS FOR MATHEMATICAL PRACTICE**

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

**BACKGROUND KNOWLEDGE**

First graders might have informally encountered negative numbers in their lives, so they think they can take away more than the number of items in a given set, resulting in a negative number below zero. Provide many problems situations where students take away all objects from a set, e.g. $19 - 19 = 0$ and focus on the meaning of 0 objects and 0 as a number. Ask students to discuss whether they can take away more objects than what they have. (N.C. Dept. of Public Instruction)
ESSENTIAL QUESTIONS

• How can we show that addition and subtraction are related?
• How can we use different combinations of numbers and operations to represent the same quantity?
• How can decomposing a number help you?

MATERIALS

• Lots of Dots blackline master
• Copy one set of 6 ladybugs for each student
• Student math journals
• How Many Counters Game
• Small Counters

GROUPING

whole/partner/small group task

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Students will explore finding sums, forming equations, expressions, and the Commutative Property.

Place the ladybugs (cut apart) in an envelope. Have the students count the number of dots on the ladybugs. Ask, “How many ways can you put the ladybugs together to make three, four, or five?” Discuss the different ways that the ladybugs can be put together and record the student’s responses on chart paper, as they record classmate responses in their personal math journals. Be sure to point out the variety of ways the students are coming up with. They may discover that one and two are the same as two and one. Encourage the discussion and allow students to create their own rule.

Continue by having them find as many number combinations for 6, 7, and 8 as they can. They will write expressions to match their number combinations. A possible solution might be: 7 is 3+4, 2+5, 1+2+4, 0+3+4, 0+2+5. End by having students write in their journal about the number 9.
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Part II
Begin to pose situations where dots are missing. For example, “All together the ladybugs have 4 spots. If one has 3 dots, how many does the other ladybug(s) have?” Record the equation $3 + \square = 4$. Provide students with additional “missing dots” questions and have them record and solve the equations in their math journals.

Part III
Students combine envelopes of ladybugs to represent larger quantities. They will continue to write equations with and without missing dots. They will also have opportunities to put together more than two addends.

Part IV
Students should play the game, How Many Counters? This partner game was created to increase proficiency with number combinations. Students will need blank ten-frames, counters and a number cube. One player secretly arranges some counters on a ten-frame. The other player asks questions that can be answered “yes” or “no”, trying to gain enough clues to work out the arrangement of counters. For example: Is the top row full? Are there 8 counters? Is there an empty box in the bottom row? As players become more skilled, the number of questions can be counted. The player asking fewer questions wins.

FORMATIVE ASSESSMENT QUESTIONS

- Is there another way that you could make the number?
- How did you determine the missing addend?
- Are you sure that you have found them all? Why do you think so? How do you know?
- Did you identify any patterns or rules? Explain!

DIFFERENTIATION

Extension

- Provide students with problems involving two expressions where one has a missing addend. For example: There were two windows with two ladybugs on each window. Both sets of ladybugs have the same number of spots. If one window has ladybugs with three spots and four spots, and the other window has one ladybug with 2 spots, how many spots does the other ladybug have? Write an equation to solve this problem.

Intervention

- Complete this task in a smaller setting. Students may work in pairs and the sum may not be greater than five. Gradually increase the sum until the concept is grasped.
Lots of Dots
How Many Counters?

Materials: Blank ten-frames, one or more per player
Counters
A number cube

Players: Two

Rules: One player secretly arranges some counters on a ten-frame. The other player asks questions that can be answered yes or no, trying to gain enough clues to work out the arrangement of counters. For example: Is the top row full? Are there 8 counters? Is there an empty box in the bottom row?

Variation: As players become more skilled, the number of questions can be counted. The player asking fewer questions wins.
How Many Counters?
CONSTRUCTING TASK: What Numbers Can You Make?

Approximately 1 day

*Adapted from Developing Number Concepts, Addition and Subtraction

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.3. Apply properties of operations as strategies to add and subtract. Examples: If 8 + 3 = 11 is known, then 3 + 8 = 11 is also known. (Commutative property of addition.) To add 2 + 6 + 4, the second two numbers can be added to make a ten, so 2 + 6 + 4 = 2 + 10 = 12. (Associative property of addition.)

MCC.1.OA.4. Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.

MCC.1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

MCC.1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 – 4 = 13 – 3 – 1 = 10 – 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 – 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

MCC.1.MD.4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

The goal of this activity is for students to understand number combinations. There may be multiple ways to represent a number, but listen for how the students explain themselves.
ESSENTIAL QUESTIONS

- How can we show that addition and subtraction are related?
- How can we use different combinations of numbers and operations to represent the same quantity?
- How can decomposing a number help you?

MATERIALS

- Connecting cubes
- What Number Can You Make- Recording Sheet
- I Spy Addition- Game
- Deck of Playing Card

GROUPING

Depending on the story problem, this task could be solved with students working as a whole-class, small groups, or independently.

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part 1
Make 5 stacks of connecting cubes, each stack a different color and having no more than 5 cubes. Show your five stacks to the class and have them build the same stacks to match yours. For example:

“Build these stacks exactly like mine.”

The object of this activity is to find out which numbers it is possible for children to combine using these stacks singly and in combination. The students may use more than one stack to
achieve their goal number, but they should not physically connect two stacks, nor should
disassemble a stack.

Once the group has built their five stacks, give them a number to create. Begin by asking
them, “Can you pick up four?” Most of your students will achieve this by picking up the red
stack. Then ask the students if there are any other ways that they can pick up four. You are
looking for students to pick up more than more stack, such as the orange and blue stacks or
the yellow and green stacks. Ask your students to show example how they know that they
have picked up the correct number. This will help them to communicate their strategies and
to reinforce the Standards for Mathematical Practice. Expected responses could be, “The
yellow stack has two and the green stack has two. Two and two makes four cubes.

Continue this practice building other numbers, each time recording the number sentences on
the anchor chart.

This activity can be done over and over using different combinations of stacks. Pose
questions such as:

- What happens if you didn’t have a “one” stack?
- What would happen if all the stacks had the same number of cubes?
- What is the largest number we could make?
- What is the smallest number we could make?

Part II
Have the students repeat the activity using their five cube trains to make each of the
numbers from one to ten in as many ways as possible. However, this time, have them record
their results by making a table on the “What Numbers Can You Make?” recording sheet. If
they can’t make a particular number, they do not fill in anything for that number. If they can
make the number, they record each combination they use to make it, example 2+3. Note that
some combinations will be repeated if children have different colored trains of the same
length.

Part III
Students should work with a partner to play, I Spy Addition to increase fluency with addition.
Students will need a deck of playing cards, with face cards removed. Aces will count as 1.
Arrange the cards face up in 5 rows with each row containing 8 cards. Player one will find a
number combination and tell player two ONLY the sum. I spy two cards that add to 12. Player
two looks for 2 cards next to each other, horizontally, vertically or diagonally that create a
combination with the same sum that player one saw. It does not have to be the exact match that
player one spotted, as long as the combination shares the same sum. If player two finds the
combination, they get to pick up the cards. If player two cannot find the combination, player one
gets to pick up the cards. As cards are picked up, the remaining cards are shifted to fill in the
spaces. Play will continue until all that cards have been collected. The winner is the player with the most cards.

**FORMATIVE ASSESSMENT QUESTIONS**

- According to your graph, which numbers are you able to create the most ways? Why do you think that is?
- What number did you use often to construct larger numbers?
- Does your graph look like your neighbors? Why do you think?

**DIFFERENTIATION**

**Extension**
- Have students work with more cube trains, giving them more variety in their number.
- Allow students to go above 10.

**Intervention**
- Have the students us a smaller number of cube trains. This will limit the variety of ways to create a number.
- Begin with only making combinations of numbers up to five.
What Numbers Can You Make?

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I Spy Combinations - Addition

Purpose:

The purpose of this activity is to help students develop fluent recall of number combinations to 20.

Number of Players:

2 Players

What you need:

• A deck of playing cards, with face cards removed. Aces will count as 1.

What to do:

• Arrange the cards face up in 5 rows with each row containing 8 cards.
• Player one will find a number combination and tell player two ONLY the sum. *I spy two cards that add to 12*
• Player two looks for 2 cards next to each other, horizontally, vertically or diagonally that create a combination with the same sum that player one saw. It does not have to be the exact match that player one spotted, as long as the combination shares the same sum.
• If player two finds the combination, they get to pick up the cards. If player two cannot find the combination, player one gets to pick up the cards.
• As cards are picked up, the remaining cards are shifted to fill in the spaces.
• Play will continue until all that cards have been collected.
• The winner is the player with the most cards.

Extension:

• Students will create number combinations using three cards in a row.
Performance Task: Wheel Shop
Approximately 2 days Adapted from the Noyce Foundation

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC.1.OA.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Provide opportunities for students to participate in shared problem-solving activities to solve word problems. Collaborate in small groups to develop problem-solving strategies using a variety of models such as drawings, words, and equations with symbols for the unknown numbers to find the solutions. Additionally students need the opportunity to explain, write and reflect on their problem-solving strategies. The situations for the addition and subtraction story problems should involve sums and differences less than or equal to 20 using the numbers 0 to 20.

ESSENTIAL QUESTIONS

- How do you determine a missing addend?
- How can we represent a group of objects with numbers?
- How can we show and explain our thinking?
**TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION**

**Part I**
Gather all students to a common area. Ask, “What do we call this? (show a picture of a bicycle) How many wheels does a bicycle have? Who can show me how they know there are two wheels? What if I have two bicycles, how many wheels would I have?” Allow students to come up with an answer and share their strategies for determining the number of wheels.

Next, the teacher shows a picture of a go-cart, and asks, “What do we call this? How many wheels does a go-cart have? What if I had two go-carts?” Allow for responses and discuss the strategies used to determine how many wheels.

**Part II**
Using drawings, equations, and written responses, students work cooperatively or independently to solve.

The Wheel Shop sells bicycles and go-carts. Each bicycle has only one seat and each go-cart has only one seat. There are a total of 7 seats and 18 wheels in the shop.

How many are bicycles and how many are go-carts? Explain how you figured it out.

**Part III**
Students should work with partners or within small groups of 4 to play Make Twenty Game. Groups will need 4 sets of 0-20 cards. Each player is dealt three cards and the rest of the cards are placed in a face down pile. The first player picks up a card from the pile and checks to see if he is able to make 20 and still discard one card. If he cannot, he discards a card (face up) and player two picks up a card from the face down pile or picks up the top card in the discard pile. The first player to make 20 wins.
FORMATIVE ASSESSMENT QUESTIONS

- How did you know the number of bicycles? Go-carts?
- What strategy did you use to determine this?
- Can you write an equation/number sentence to show your thinking?
- Is this the only solution? How do you know?

DIFFERENTIATION

Extension
- To extend their thinking include a tricycle. There could be 5 seats and 19 wheels.

Intervention
- Provide students with the amount of bicycles and go-carts, and ask them to determine the number of wheels.
The Wheel Shop sells bicycles and go-carts. Each bicycle has only one seat and each go-cart has only one seat. There are a total of 7 seats and 18 wheels in the shop.

How many are bicycles and how many are go-carts?

Use pictures, words, and numbers to show your math thinking.
Make Twenty

Skills/concepts: Addition

Materials: 4 sets of number cards (0 to 20)

Number of Players: 2 to 4

Directions: Each player is dealt three cards and the rest of the cards are placed in a face down pile. The first player picks up a card from the pile and checks to see if he is able to make 20 and still discard one card. If he cannot, he discards a card (face up) and player two picks up a card from the face down pile or picks up the top card in the discard pile. The first player to make 20 wins.

Variation 1: Deal 8 cards to each player and try to make as many combinations that make 20 as possible. Combinations can be put down as soon as they are made. The game ends when one player has no cards left after discarding one and putting down the combinations to 20. Winner has the most sets to make 20.

Variation 2: Change the target sum to a number between 10 and 20.
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PERFORMANCE TASK: Digging Dinosaurs
Approximately 1 day    Adapted from the Noyce Foundation

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC.1.OA.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Provide opportunities for students to participate in shared problem-solving activities to solve word problems. Collaborate in small groups to develop problem-solving strategies using a variety of models such as drawings, words, and equations with symbols for the unknown numbers to find the solutions. Additionally, students need the opportunity to explain, write and reflect on their problem-solving strategies. The situations for the addition and subtraction story problems should involve sums and differences less than or equal to 20, using the numbers 0 to 20.

ESSENTIAL QUESTIONS

• How does decomposing a number help you in a problem solving situation?
• How do number sentences help you explain your thinking?
• How can we represent a number in a variety of ways?
MATERIALS

- Digging Dinosaurs Blackline Master
- Pencil and paper
- Digging Dino Water Template
- Ten Frame
- Counters

GROUPING

small group/partners/individual

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Gather students in a common area. (Teacher holds up the picture) “Tell me about this picture? What do you see?” (Teacher solicits answers from students) “How many dinosaur feet do you see in this picture?” How many legs does a dinosaur have? Which dinosaurs have 2 legs? Which dinosaurs have 4 legs? Are there any other dinosaurs with a different number of legs? How many dinosaurs are standing in the lake? Explain why you think it would be that number. Can you draw a complete drawing of the dinosaurs standing in the lake? Can you show how you got your answer? (At the end of the investigation have students either discuss or dictate a response to the summary questions). (Teacher solicits answers from students and then states that the class will investigate this question) “We are going to try and figure out how many dinosaurs are standing in the lake.”

Using drawings, equations, and written responses, students work cooperatively or independently to solve.

How many dinosaurs are standing in the lake? Explain why you think it would be that number. Can you illustrate a complete drawing of the dinosaurs standing in the lake? Can you show how you got your answer? (At the end of the investigation have students either discuss or dictate a response to the summary questions). (Teacher solicits answers from students and then states that the class will investigate this question) “We are going to try and figure out how many dinosaurs are standing in the lake.”

Part II
Students will create their own problem using the Digging Dino Water Template. They will then exchange their problems with a partner. Give students the opportunity to share with the class.
Part III
Students should play *Ten Frame Flash* in small groups for further practice with addition and subtraction. The first player shows a ten-frame for a count of three, then hides it while the other players place counters in the same positions on their frames from memory. The 'flasher' shows the card again and helps each player check his/her display. After three cards the next player becomes the 'flasher' and so on, until everyone has had a turn.

**QUESTIONS FOR FORMATIVE STUDENT ASSESSMENT**

- How many dinosaurs are standing in the lake?
- Explain why you think it would be that number.
- Can you draw a complete drawing of the dinosaurs standing in the lake?
- Can you show how you got your answer?

**DIFFERENTIATION**

**Extension**
- Add additional dinosaur legs, have students describe what has changed and how their solution has changed.
- Find an additional solution, using different number combinations.

**Intervention**
- Allow students to complete problem using manipulatives in a one-on-one interview-style setting.
You are swimming under water in a lake and you see dinosaur feet in the water. You don’t want to go to the surface in case they are not friendly dinosaurs. Below is a picture of what you see.

How many dinosaurs are standing in the lake?
Explain how you know. Use words and mathematical language to explain your solution.
Ten Frame Flash

Materials: Ten-frames with dot arrangements
          Counters
          A blank ten-frame for each player

Players: four

Rules: The first player shows a ten-frame for a count of three, then hides it while the other players place counters in the same positions on their frames from memory. The 'flasher' shows the card again and helps each player check his/her display. After three cards the next player becomes the 'flasher' and so on, until everyone has had a turn.

Variation 1: Points can be awarded for each correct response. The player with the most points wins.

Variation 2: This game can be played as a whole class with one student using overhead versions of the filled ten frames to flash for the whole class.

Variation 3: A more difficult addition game can be played by flashing two ten frames at a time and having students show the sum of the two ten frames on one ten frame (or two if the sum is greater than 10).

Variation 4: A more difficult subtraction game can be played by flashing two ten frames at a time and having students show the difference on one ten frame.

This activity was adapted from: http://www.nrich.maths.org.uk/prime/may99/staff.htm
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MATHEMATICS • GRADE 1 • UNIT 5: Operations and Algebraic Thinking
Georgia Department of Education
Dr. John D. Barge, State School Superintendent
May 2012 • Page 52 of 92
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CONSTRUCTING TASK: Developing Meaning by using Story Problems: Change Unknown

Approximately 2-3 days

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

The goal for this lesson is to revisit real world problems, using the level of understanding (concrete, representational, or abstract) that each student needs. (see CRA Table on page 15) Addition and subtraction can be divided into four categories: join problems, separate problems, part-whole problems, and compare problems (see Table 1 on page 8). Within these four types of problems, most educators focus on addition and subtract when the result is unknown, this leads to the understanding that addition is “put together” and subtraction means to “take away”. This is a major misconception and limits the students’ understanding. One way to prevent development of this misunderstanding is to provide problem based story problems in which the students are attempting to solve not only the result but also the change, and the initial.

Students should not complete a multitude of problems within one class period, rather they should work in depth with as few as one problem that they can know and understand completely. Students do not need to know the names of the different types of problems but they should have experience in solving all of the different types. This lesson should not be looked at to be completed in one session, these questions should be readdressed throughout this unit and continue throughout the mathematics curriculum across grade levels.
ESSENTIAL QUESTIONS

- What happens when we join two quantities or take one from another?
- How can we find the total when we join two quantities?
- How can we find what is left when we take one quantity from another?
- What happens when we change the order of numbers when we add (or subtract)? Why?

MATERIALS

- Paper
- Various Manipulatives (examples: counters, based ten blocks, arithmetic rack, etc.)
- Pencils and crayons
- Types of Problems (cut out)
- Twenty Game
- Dice
- Small counters

GROUPING

Flexible grouping based on student needs. Depending on the story problem, this task could be solved with students working as a whole-class, small groups, or independently.

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
The teacher will tell a story similar to: Ten friends were playing outside together on a summer day. Some of the friends had to go home to eat lunch. Now there are six friends playing. How many friends went home to eat lunch?

After telling the story, suggested questions include:
- What is my story about?
- What happened first? What happened next?
- Were there more (or fewer) friends at beginning of the story or at the end of the story? How did you figure that out?
- How can we show/represent this? Can we act out the story?
- How many friends were there at the beginning of the story? (Feel free to let the students act out this situation if necessary)
- How many friends were taken away?
- How many friends were left at the end of the story? How do you know?

Continue questioning as needed until the students can answer the questions and understand what is happening in the story.
Part II
Sample problems have been provided. Copy the problems, cut them out to give to students and/or flexible groups. Each set can be done within small groups or within centers/work stations. The sample word problems are designed to give a conceptual understanding of addition and subtraction of two numbers. Students should explore these problems using the CRA model. Refer to the CRA table on page 15 for explanation and questioning.

- C- Concrete: Using Manipulatives (acting out)
- R- Representational: Drawing Pictures
- A- Abstract: Creating Number Sentences

“In the classroom, this approach is a facilitating framework for students to create meaningful connections between concrete, representational, and abstract levels of thinking and understanding. Students’ learning starts out with visual, tangible, and kinesthetic experiences to establish basic understanding, and then students are able to extend their knowledge through pictorial representations (drawings, diagrams, or sketches) and then finally are able to move to the abstract level of thinking, where students are exclusively using mathematical symbols to represent and model problems.” Hauser, Jane. Concrete-representational-abstract instructional approach. Retrieved April 9, 2009, from the Access Center: Improving Outcomes for all Students K-8. Web site: http://www.k8accesscenter.org/training_resources/CRA_Instructional_Approach.asp

The problems listed below are examples from the four types of addition/subtraction problems. The numbers and topics of each problem can be adjusted based on the interest and ability of your students. All four types of problems should be focused in a variety of ways.

Join Problems:
When joining two quantities, three different amounts are used: the initial amount, the change amount, and the result amount (or whole). (VDW)

Separate Problems:
Within separate problems, your initial amount is the whole. This differs from a joining problem because within a joining problem your result is your whole. (VDW)

Part-Part-Whole Problems:
Part-Part-Whole is the combing of two quantities to create a whole. The combination can take place physically, or it can be asked to be completed mentally.

Comparing Problems:
Comparing problems do not focus on the operation, but rather the relationship between two quantities. This relationship can be stated or it can be implied by using terms of greater than or less than. (VDW)
Comment: Teachers should expose students to a variety of separating problem types. Students do not need to know the names of the different types of problems but they should have experience in solving all of the different types.

Part III
Students will work in pairs to play the Twenty game. Each player rolls a die, places that number of counters onto his/her ten frame, then announces the total number of counters on the ten frames. Next, the player records the number sentence onto the chart below. Both players will use the same recording sheet. Example: Player one rolls a 5. He places 5 counters onto his ten frame and writes the number sentence 0+5=5. The 0 represents the number of counters on the ten frames before the roll, the 5 represents the number of counters added to the ten frames, and the 5 represents the total amount on the ten frames after the roll. Player 2 will then roll the die and do the same. On the next turn, player one rolls a 3. He place 3 counters on the tens frame and writes the number sentence 5+3=8. The 5 represents the number of counters before the roll, the 3 represents the number of counters added to the ten frames, and the 8 represents the total amount on the ten frames after the roll. Play continues until a player fills both ten frames and reaches a sum of 20.

FORMATIVE ASSESSMENT QUESTIONS
See suggested questioning located within task description and CRA Table on page 15.

DIFFERENTIATION

Extension:
• Allow students to work with numbers larger than 20 without regrouping.
• Ask students to create and solve their own story problems.

Note: Students typically create addition problems. Check students’ problems to make sure they are creating subtraction problems too.

Intervention
• Allow students to work through the stages at a pace that is appropriate to their developmental level. This will provide students with the remediation they need to understand the concept of comparing numbers. Continue to allow them to work with manipulatives as much as needed. At times, partner them with students who are very articulate about their mathematical thinking so they can hear (through conversations) how these students have made sense of the problems.
Directions:

• Each player rolls a die, places that number of counters on his/her ten frame, then announces the total number of counters on the ten frames.

• Next, the player records the number sentence onto the chart below. Both players will use the same recording sheet. Example: Player one rolls a 5. He places 5 counters on his ten frame and writes the number sentence 0+5=5. The 0 represents the number of counters on the ten frames before the roll, the 5 represents the number of counters added to the ten frames, and the 5 represents the total amount on the ten frames after the roll.

• Player 2 will then roll the die and do the same.

• On the next turn, player one rolls a 3. He place 3 counters on the tens frame and writes the number sentence 5+3=8. The 5 represents the number of counters before the roll, the 3 represents the number of counters added to the ten frames, and the 8 represents the total amount on the ten frames after the roll.

• Play continues until a player fills both ten frames and reaches a sum of 20.
Ten Frames for Twenty Game
**Twenty**

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CONSTRUCTING TASK: Shape Pounds
Approximately 2 days *Adapted from NCTM’s Navigating through Algebra P-2

STANDARDS FOR MATHEMATICAL CONTENT

MCC1.OA.7 Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? 6 = 6, 7 = 8 – 1, 5 + 2 = 2 + 5, 4 + 1 = 5 + 2.

MCC1.OA.8 Determine the unknown whole number in an addition or subtraction equation relating to three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8 + ? = 11, 5 = □ – 3, 6 + 6 = Δ.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
4. Model with mathematics.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Many students think that the equals sign means that an operation must be performed on the numbers on the left and the result of this operation is written on the right. They think that the equal sign is like an arrow that means becomes and one number cannot be alone on the left. Students often ignore the equal sign in equations that are written in a nontraditional way. For instance, students find the incorrect value for the unknown in the equation 9 = Δ – 5 by thinking 9 – 5 = 4. It is important to provide equations with a single number on the left as in 18 = 10 + 8. Showing pairs of equations such as 11 = 7 + 4 and 7 + 4 = 11 gives students experiences with the meaning of the equal sign as is the same as and equations with one number to the left.

ESSENTIAL QUESTIONS

• What does the = sign mean?
• When is it appropriate to use the equal sign?

MATERIALS

• Chart Paper
• Block Pounds Blackline Master
GROUPING

Whole group/small group/individual

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Draw a picture of two balance scales on the board labeled A and B.

Inform the students that the weight listed on the scale is the weight of the blocks. Ask them the following questions:

- (pointing) What is the object shown on scale B?
- (pointing) What are the objects shown on scale A?
- What do you think that the weight of the triangle is? How do you know?
- What do you think the weight of the square is? How do you know?
  (The triangle is 6 pounds and the square is 9-6 pounds so it’s 3)

Draw two additional scales on the board like the ones below.

Ask the following questions:

- What is the name of the object on scale A? How much does the triangle weigh?
- What are the names of the objects on scale B? How could you determine the weight of the squares (□+4+□=14)? Do not introduce the writing of the equations using the until Part II. This idea should be developed through discussion and trial and error. It’s important to work through the students thoughts as the discussion develops.
- Do the two squares weigh the same? At this point you will want to discuss that the squares will weigh the same, just as the Δ weighs the same on both scales. This will also lead them to the discussion of double, in this case, 5 and 5.
Students will be exploring variables as unknowns. They will be solving for the weights of the shapes using the information provided on the scales.

**Part II**
Distribute a copy of the recording sheet “Shape Pounds”. Have students work in pairs to determine the weight of the shapes. Have them explain how they determined the weight of each shape. The weights of the shapes will increase in difficulty as the students move through the recording sheet.

**Part III**
Work with students to develop equations representing the weight on the scales, using the same examples as in the opening. For the first example, the equation would be $9=6+\square$. It is important to reference their work in Part II and talk about the weights on both scales.

Ask the following questions:
- How did we know to put the 6 in the equation for scale A?
- Why did we add 6 to a square?
- What does the square represent?
- Why might we have put the 9 first?
- Can we write it like this $6+\square=9$?

Do the same for the other scales and develop equations with the students. Ask students to revisit the recording sheet from Part 1. Ask them to write an equation for the scales. Ask students to share their strategies for determining the weights of the objects and the equations that they wrote.

**Part IV**
Students will work with a partner to play *Whose Sum is Larger?* Deal out an entire deck of playing cards out, so that the two players have an equal number of cards. Each player will turn over two playing cards from their stack. The player will add their two cards together. The player with the larger sum gets all four cards. If the two players have a tie, the players will turn over an additional card to add to their sum as a “tie breaker”. The player with the most cards wins, once players have gone through the entire deck.

**FORMATIVE ASSESSMENT QUESTIONS**

- What is the weight of the shape (pointing to a particular shape)? How did you determine the weight of the object?
- How can you write an equation/number sentence to represent the weight on the scale?
DIFFERENTIATION

Extension:
• Students who are able to easily find the unknown and write equations using the variables, can balance the scales. For example, if one scale equals 9 and the other 14, how can we make them equal? What could we add to the 9 to make it fourteen?

Intervention
• Teacher can work with students in small groups using smaller numbers, with no more than two shapes, or use color tiles to represent pound amounts, allowing students to confirm quantities.
Shape Pounds

Name:_____________________   Date:________________

Shape Pounds

= ____

= ____

= ____

= ____

= ____

= ____

= ____

= ____
Whose Sum is Larger???

**Materials Needed:**
Playing Cards

**Number of Players:**
Partners

**Directions:**
- Deal the entire deck of playing cards out, so that the two players have an equal number of cards.
- Each player will turn over two playing cards from their stack. The player will add their two cards together.
- The player with the larger sum gets all four cards.
- If the two players have a tie, the players will turn over an additional card to add to their sum as a "tie breaker".
- Once players have gone through the entire deck, the player with the most cards wins.

**Variations:**
- Have students go through the deck multiple times.
- Have students play Whose Sum is Smaller.
SCAFFOLDING TASK: Fact Families to 10
Approximately 1-2 days
* Adapted from Hands On Standards, Grades 1-2

MCC.1.OA.3. Apply properties of operations as strategies to add and subtract.
Examples: If 8 + 3 = 11 is known, then 3 + 8 = 11 is also known. (Commutative property of addition.) To add 2 + 6 + 4, the second two numbers can be added to make a ten, so 2 + 6 + 4 = 2 + 10 = 12. (Associative property of addition.)

MCC.1.OA.4. Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.

MCC.1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

MCC.1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 – 4 = 13 – 3 – 1 = 10 – 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 – 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

STANDARDS FOR MATHEMATICAL PRACTICE
1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE
Fact families provide a method for children to compute fluently with whole numbers. Addition and subtraction fact families help children develop number sense as they see the relationship among numbers and between the operations. During grades 1 and 2, children should begin to shift from computing mentally to using pencil and paper. At the same time, mental math skills such as grouping and estimating continue to develop. Using fact families helps children develop these skills as they discern how numbers relate parts to a whole.
ESSENTIAL QUESTIONS

• How can we show that addition and subtraction are related through fact families?
• What happens when we join two quantities or take one from another?
• How can we find the total when we join two quantities?
• How can we find what is left when we take one quantity from another?

MATERIALS

• Connecting cubes
• Toy Boxes Recording Sheet
• Double Dice or Two dice
• Double Dice Addition/Subtraction Recording Sheet

GROUPING

Depending on the story problem, this task could be solved with students working as a whole-class, small groups, or independently.

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Introduce the problem:
Mrs. Cloud’s class is making boxes of toys to give to a preschool. Each box can have 4, 5, 6, 7, 8, 9, or 10 toys. Each box will have dolls and trucks. How many dolls and trucks can be in each box?
Assign each student/group the number toys in the toy box. This is a perfect time to differentiate for students that would need to work numbers on their level. Then have them draw a picture of the dolls and the trucks within their toy box. At this time, have the students explain why they need that many dolls or that many trucks. This is a good time to assess if the students have an accurate number combination for their assigned number of toys in the toy box.

Part II
During this task, the students will use the number of dolls and trucks that they created in the opening to build a fact family. The students will first build the family with connecting cubes and then write corresponding number sentences.
Ask children to make a train of connecting cubes using two different colors. The total number of cubes in the train should be the same as the number of toys in their toy box. One color should represent the number of dolls, and one color should represent the number of trucks. Then explain to the students that the dolls and trucks have switched, and they need to create a second train to represent the new number of each toy.

Help the children to create two addition sentences that describe their trains. Then, help them create two subtraction sentences that show what happens to the total if one color (or toy) is removed from the toy box. Lead children to discover that the same three numbers appear in all the number sentences, but do not explicitly tell them this. Once a student has discovered this pattern, explain to the class that this is called a fact family.

Encourage the students to find a different number of dolls and trucks that could still fit in their toy box.

**Part III**
Students should play the Double Dice Addition Activity and Double Dice Subtraction Activity for further practice to build fluency.

**FORMATIVE ASSESSMENT QUESTIONS**

- Do you see any similarities in your number sentences?
- Do you see any differences?
- Why do you think three numbers make up a fact family?

**DIFFERENTIATION**

**Extension**
- Create a fact family for a number sentence with an unknown.
- Allow students to choose the number of toys in their toy box, within their ability level.

**Intervention**
- Begin with 4 toys total in the toy box.
- Use a different visual such real dolls and trucks, or red and yellow counters.
Toy Boxes

Mrs. Cloud’s class is making boxes of toys to give to a preschool. Each box can have 4, 5, 6, 7, 8, 9, or 10 toys. Each box will have dolls and trucks. How many dolls and trucks can be in each box?
Double Dice Addition

Roll the double dice. Add the two numbers and record the number sentence. If no double dice are available then use two 6-sided dice.

1. ______  ______ = __________

2. ______  ______ = __________

3. ______  ______ = __________

4. ______  ______ = __________

5. ______  ______ = __________

6. ______  ______ = __________

7. ______  ______ = __________

8. ______  ______ = __________

9. ______  ______ = __________

10. ______  ______ = __________

11. ______  ______ = __________

12. ______  ______ = __________

13. ______  ______ = __________

14. ______  ______ = __________
Double Dice Subtraction

Roll the double dice. Subtract the two numbers and record the number sentence. Make sure the greater number is first. If no double dice are available then use two 6-sided dice.

1. _____ _____ = _______

2. _____ _____ = _______

3. _____ _____ = _______

4. _____ _____ = _______

5. _____ _____ = _______

6. _____ _____ = _______

7. _____ _____ = _______

8. _____ _____ = _______

9. _____ _____ = _______

10. _____ _____ = _______

11. _____ _____ = _______

12. _____ _____ = _______

13. _____ _____ = _______

14. _____ _____ = _______
CONSTRUCTING TASK: Developing Meaning by Using Story Problems: Initial Unknown

Approximately 2-3 days

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

The goal for this lesson is to revisit real world problems, using the level of understanding (concrete, representational, or abstract) that each student needs. (see CRA Table on page 15) Addition and subtraction can be divided into four categories: join problems, separate problems, part-whole problems, and compare problems (see Table 1 on page 8). Within these four types of problems, most educators focus on addition and subtract when the result is unknown, this leads to the understanding that addition is “put together” and subtraction means to “take away”. This is a major misconception and limits the students’ understanding. One way to prevent development of this misunderstanding is to provide problem based story problems in which the students are attempting to solve not only the result but also the change, and the initial.

Students should not complete a multitude of problems within one class period, rather they should work in depth with as few as one problem that they can know and understand completely. Students do not need to know the names of the different types of problems but they should have experience in solving all of the different types. This lesson should not be looked at to be completed in one session, these questions should be readdressed throughout this unit and continue throughout the mathematics curriculum across grade levels.
ESSENTIAL QUESTIONS

- What happens when we join two quantities or take one from another?
- How can we find the total when we join two quantities?
- How can we find what is left when we take one quantity from another?
- What happens when we change the order of numbers when we add (or subtract)? Why?

MATERIALS

- Paper
- Various Manipulatives (examples: counters, based ten blocks, arithmetic rack, etc.)
- Pencils and crayons
- Types of Problems (cut out)
- Doubles Memory Game

GROUPING

Flexible grouping based on student needs. Depending on the story problem, this task could be solved with students working as a whole-class, small groups, or independently.

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
The teacher will tell a story similar to: Some friends were playing outside together on a summer day. Two of the friends had to go home to eat lunch. Now, there are six friends playing. How many friends were outside playing together?

After telling the story, suggested questions include:
- What is my story about?
- What happened first?
- What happened next?
- Were there more (or fewer) friends at beginning of the story or at the end of the story? How did you figure that out?
- How can we show/represent this? Can we act out the story?
- How many friends were there at the beginning of the story? (Feel free to let the students act out this situation if necessary)
- How many friends were taken away?
- How many friends were left at the end of the story?
- How do you know?

Continue questioning as needed until the students can answer the questions and understand what is happening in the story.
Part II
Sample problems have been provided. Copy the problems, cut them out to give to students and/or flexible groups. Each set can be done within small groups or within centers/work stations. The sample word problems are designed to give a conceptual understanding of addition and subtraction of two numbers. Students should explore these problems using the CRA model. Refer to the CRA table on page 15 for explanation and questioning.

- C- Concrete: Using Manipulatives (acting out)
- R- Representational: Drawing Pictures
- A- Abstract: Creating Number Sentences

“In the classroom, this approach is a facilitating framework for students to create meaningful connections between concrete, representational, and abstract levels of thinking and understanding. Students’ learning starts out with visual, tangible, and kinesthetic experiences to establish basic understanding, and then students are able to extend their knowledge through pictorial representations (drawings, diagrams, or sketches) and then finally are able to move to the abstract level of thinking, where students are exclusively using mathematical symbols to represent and model problems.” Hauser, Jane. Concrete-representational-abstract instructional approach. Retrieved April 9, 2009, from the Access Center: Improving Outcomes for all Students K-8. Web site: http://www.k8accesscenter.org/training_resources/CRA_Instructional_Approach.asp

The problems listed below are examples from the four types of addition/subtraction problems. The numbers and topics of each problem can be adjusted based on the interest and ability of your students. All four types of problems should be focused in a variety of ways.

Join Problems:
When joining two quantities, three different amounts are used: the initial amount, the change amount, and the result amount (or whole). (VDW)

Separate Problems:
Within separate problems, your initial amount is the whole. This differs from a joining problem because within a joining problem your result is your whole. (VDW)

Part-Part-Whole Problems:
Part-Part-Whole is the combing of two quantities to create a whole. The combination can take place physically, or it can be asked to be completed mentally.

Comparing Problems:
Comparing problems do not focus on the operation, but rather the relationship between two quantities. This relationship can be stated or it can be implied by using terms of greater than or less than. (VDW)
Part III
Students will play *Sums of 10 Memory*. The purpose of this activity is for students to build their fluency of number combinations to ten. Students will play in groups of 2-4 and each group will need a deck of cards. This is a game played like Memory. The cards are first spread out in an organized array with all cards face down. The first person turns over two cards, without moving them from original location. If the two cards showing create a number combination of ten, the player takes the pair and has another turn. If the cards do not create a number combination of ten, they turn the cards back over face down. The next player has a turn. The winner is the player with the most pairs.

**FORMATIVE ASSESSMENT QUESTIONS**

See suggested questioning located within task description and CRA Table on page 15.

**DIFFERENTIATION**

**Extension:**
- Allow students to work with numbers larger than 20.
- Ask students to create and solve their own story problems.

  Note: Students typically create addition problems. Check students’ problems to make sure they are creating subtraction problems too.

**Intervention**
- Allow students to work through the stages at a pace that is appropriate to their developmental level. This will provide students with the remediation they need to understand the concept of comparing numbers. Continue to allow them to work with manipulatives as much as needed. At times, partner them with students who are very articulate about their mathematical thinking so they can hear (through conversations) how these students have made sense of the problems.
Sums of Ten Memory

Purpose:

The purpose of this activity is for students to build their fluency of number combinations to ten.

How children will be organized:

Students will play in groups of 2-4

What you need:

Playing cards:
- A: Aces= 1
- 2-10= their numerical value
- J-K (all face cards)= 10

What to do:
This is game is played like Memory. The cards are first spread out in an organized array with all cards face down. The first person turns over two cards, without moving them from original location. If the two cards showing create a number combination of ten, the player takes the pair and has another turn. If the cards do not create a number combination of ten, they turn the cards back over face down. The next player has a turn. The winner is the player with the most pairs.
Practice Task: Domino Fact Families
Approximately 1 day (adapted from Mathwire.com)

STANDARDS FOR MATHEMATICAL CONTENT

MCC.1.OA.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14); decomposing a number leading to a ten (e.g., 13 – 4 = 13 – 3 – 1 = 10 – 1 = 9); using the relationship between addition and subtraction (e.g., knowing that 8 + 4 = 12, one knows 12 – 8 = 4); and creating equivalent but easier or known sums (e.g., adding 6 + 7 by creating the known equivalent 6 + 6 + 1 = 12 + 1 = 13).

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Success in this task depends on students understanding that once they can recall a particular addition fact, they can use that fact to solve a variety of related addition and subtraction tasks. The set of related facts is called a family. Before this, students will see number facts as unrelated, and hence might feel burdened by how many facts there are to learn. The use of fact families can help students to see relationships between several addition and subtraction facts.

ESSENTIAL QUESTIONS

- How can we show that addition and subtraction are related through fact families?
- What happens when we join two quantities or take one from another?
- How can we find the total when we join two quantities?
- How can we find what is left when we take one quantity from another?
MATERIALS
- One bag of dominos per student (approximately 8 within each bag), or domino cut-outs (see K units for domino masters)
- Domino Fact Family Recording Sheet
- Ten Wins!
- Dice
- Counters

GROUPING
Individual

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Part I
Gather students to a common area. Draw several demonstration dominos on the board. You can also make large demonstration dominos by cutting a piece of poster paper in half and drawing dots on either side. Ask students to look at both halves of the domino and tell how many dots are in each square. Suggested questions include:

- What is the sum if you add the dots in each square?
- Will the sum change if I flip the domino (180 degree turn)? Why do you think this? (Special Note: This is not about students understanding degrees and angles. It is included for teachers to identify the specific way to flip the domino.)
- Is there another way we could write the addition sentence and still get the same sum?
- What would the difference be if you subtracted the number of dots in one of the squares from the sum?
- What type of relationship are you noticing?
- What are the number sentences in the fact family for this domino?

Part II
Allow children to work independently to record the fact families that their dominos show. They will need to draw each domino and label it with their fact family using the recording sheet. Observe the counting strategies that the children utilize. Notice if they are counting on, counting each individual dot, or recalling the answers because they know their addition and subtraction facts. (Note: Students are only being exposed to the concepts of vertical and horizontal. It is not the focus of the task, but teachers are encouraged to use the terms in vocabulary. Students are not responsible for this yet.)

Allow several students to share their work. Allow students to discuss how they determined the number sentences in their fact family and the strategies they used to create these number sentences. Allow time for the student who is sharing to answer questions, receive compliments, and listen to suggestions from the audience.
Part III
Students will play, *Ten Wins!* with a partner. Each player will need 10 counters of one color. Player one will roll the dice and add the two numbers to find the sum. Cover the sum with their designated color counter. Player two will roll the dice and add the two numbers to find the sum. They will also cover the sum with their designated color counter. If a space is already covered by the opponent’s counter, then a player may steal that spot. Example: Player one has a blue counter on the number 9. Player two rolls a 5 and 4. Player two may remove the blue counter and place their color counter on that space. The first player to use all ten counters on the game board wins!

**FORMATIVE ASSESSMENT QUESTIONS**

- How many dots are on the left side of your domino (looking at it horizontally)?
- How many dots are on the top of your domino (looking at it vertically)?
- How many dots are on the right side of your domino (looking at it horizontally)?
- How many dots are on the bottom of your domino (looking at it vertically)?
- What is the sum if you add the dots in each of your domino squares?
- Is there another way you could write the addition sentence and still get the same sum?
- What would the difference be if you subtracted the number of dots in one of the squares from the sum?
- What are the numbers in this fact family?
- What type of relationship are you noticing?
- What are the number sentences in the fact family for this domino?
- How are you determining the fact families for each of your dominoes?
- Why is it important to know fact families?

**DIFFERENTIATION**

**Extension**
- Allow students to create their own fact families with larger numbers.

**Intervention**
- Give students note cards that have an addition or subtraction number sentence written on each card. Have students group the cards into fact families. Once they get the hang of this, give them three of the four number sentences and they have to figure out the one that is missing. As they get better with the game start decreasing the number of sentences you give them. Once they can tell you three of the sentences when you have only given them one, change the game. You give them all the number sentences in the family and they have to tell you who the individual family members are.

**Technology Connection**
- This Smart Board activity provides additional practice with adding the pips on a domino. [http://exchange.smarttech.com/details.html?id=48909ccd-c54a-4281-aaea-91faf0f33354](http://exchange.smarttech.com/details.html?id=48909ccd-c54a-4281-aaea-91faf0f33354)
### Domino Fact Family Recording Sheet

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<td></td>
</tr>
</tbody>
</table>

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### Instructions
- Fill in the blanks with numbers to complete the fact families.
- Each domino represents a fact family with two addition and two subtraction facts.
- Use the numbers provided in the domino to complete the equations.

---

**Example:**
- If the domino shows 3, 2, and 5, then the equations could be:
  - $3 + 2 = 5$
  - $2 + 3 = 5$
  - $5 - 2 = 3$
  - $5 - 3 = 2$

---

**Note:** Ensure each domino has two numbers that can form a valid fact family.
Ten Wins!

Directions: Ten Wins! is a partner game. Each player will need 10 counters of one color. Player one will roll the dice and add the two numbers to find the sum. Cover the sum with their designated color counter. Player two will roll the dice and add the two number to find the sum. They will also cover the sum with their designated color counter. If a space is already cover by the opponents counter then a player may steal that spot. Example: Player one has a blue counter on the number 9. Player two rolls a 5 and 4. Player two may remove the blue counter and place their color counter on that space. The first player to use all ten counters on the game board wins!
Practice Task: Candy

STANDARDS FOR MATHEMATICAL CONTENT

MCC1.MD.4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

MCC1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

This standard calls for students to work with categorical data by organizing, representing and interpreting data. Students should have experiences posing a question with 3 possible responses and then work with the data that they collect. For example:

Students pose a question and the 3 possible responses: Which is your favorite flavor of ice cream? Chocolate, vanilla or strawberry? Students collect their data by using tallies or another way of keeping track. Students organize their data by totaling each category in a chart or table. Picture and bar graphs are introduced in 2nd Grade.

<table>
<thead>
<tr>
<th>What is your favorite flavor of ice cream?</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Chocolate</td>
<td>12</td>
</tr>
<tr>
<td>Vanilla</td>
<td>5</td>
</tr>
<tr>
<td>Strawberry</td>
<td>6</td>
</tr>
</tbody>
</table>

ESSENTIAL QUESTIONS

• How do tables help you organize your thinking?
MATERIALS

- Snack size packs of Skittles or M&Ms, (one bag for each pair of students or small group) (may substitute buttons, or color tiles)
- Paper and pencils

GROUPING

Whole class/small group/partners

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Let students know that they will be collecting data on the different colors in the bag of M&Ms/Skittles. Ask the students to name the colors that they may find in the bag. Write the list on the board. Take a survey asking the class to vote for their favorite color. Display the data in a table using numbers or tallies. Ask the students to identify the 3 colors that were liked the best. Pose the questions, “Which color do the most students like?” “What is the second and third favorite in the class?” After each question have them explain how they knew that it was a favorite.

Part II
Students will be organizing data into three categories (the three favorite colors chosen in the opening). They will use the snack size bags to record the amount of each color that they bag contains.
Provide each pair of students with a snack size bag of M&Ms or Skittles. Instruct students to open the bag and pull the colors out that were decided in the opening (the three favorite colors). Students will count and record the amount of each of the three colors in a table.

Pose the following questions to the students:
- Which color has the most? How do you know?
- Which color has the least? How do you know?
- How can you figure out if a color has more or less?
- How many more of color A than of color B or C? How do you know?
- Do you think that all of the bags will have the same amount of each color? Why?
- How many of A, B, and C do you have?
- Is it more or less than 20? How many more would you need to make 20? How do you know?

Have students ask classmates these same questions.
FORMATIVE ASSESSMENT QUESTIONS

See questions suggested within task description.

DIFFERENTIATION

Extension:
• Allow students to create a table that represents all of the colors in the bag. Pose the same questions.

Intervention
• Allow students to place the candies on ten frames when determining the sums and differences.
Culminating Task: Atlanta Zoo
Approximately 1 day

STANDARDS FOR MATHEMATICAL CONTENT

MCC1.MD.4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

MCC1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.

MCC1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

STANDARDS FOR MATHEMATICAL PRACTICE

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

In order to complete this culminating activity, students should have had prior experiences reading and creating tally charts and tables. They should have also had opportunities to work through several types of problem solving activities using the C-R-A model and working with three addends.

ESSENTIAL QUESTIONS

- How do tables help us organize our thinking?
- How are the properties of addition useful when problem solving?
MATERIALS

- Paper and pencils
- Manipulatives such as linking cubes, or counters
- *Animals on Board* by Stuart J. Murphy or a similar animal book
- Atlanta Zoo Recording Sheet

GROUPING

Individual

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Part I
Read *Animals on Board* by Stuart J. Murphy or a similar animal book. After reading the book ask students the following questions:

- What if we only knew the total number of Animals?
- How could we determine how many of each kind?

Allow them to share and model their thoughts.

Part II
Students will be using and creating tables/tally charts, as well as working with a sum and discovering the various addends to solve the problem. The students will come up with a variety of solutions. They will be demonstrating their ability to reason through a problem.

The Atlanta Zoo will be receiving 16 new animals. Some are zebras, some are chimpanzees, and some are giraffes. How many of each kind could they be receiving? Find as many combinations as you can. Use data tables to record your responses. Answers will vary.

FORMATIVE ASSESSMENT QUESTIONS

- Is there another combination for the zoo animals?
- Have you found all of the possibilities? How do you know?
- How many more of animal A do you have in this table than animal B or C?
- How did you know the total of each animal?
- How does creating a table help you determine your addends?
DIFFERENTIATION

Extension
• Students could be given a greater sum, or amount of animals.
• Write and solve their own story problem with three or more addends.

Intervention
• Provide manipulatives or paper cut outs of animals
• Students can use only two types of animals.
• They can act out the scenario in a one-on-one interview with the teacher.
The Atlanta Zoo

The Atlanta Zoo will be receiving 18 new animals. Some are zebras, some are chimpanzees, and some are giraffes. How many of each kind could they be receiving? Find as many combinations as you can. Use data tables to record your responses.